

Math 10B with Professor Stankova

Quiz 13; Tuesday, 4/24/2018

Section #203; Time: 9:30 AM

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Circle True or False or leave blank. (1 point for correct answer,  $-1$  for incorrect answer,  $0$  if left blank)

1. True    False    If  $\det(A) = 0$ , we need to use Gaussian elimination to determine if  $A\vec{v} = \vec{0}$  has  $0$  or  $\infty$  solutions.
2. True    False    If  $\det(A) = 0$ , then  $0$  is an eigenvalue for  $A$ .

Show your work and justify your answers. Please circle or box your final answer.

3. (10 points) (a) (6 points) Let  $A = \begin{pmatrix} 0 & -1 & 2 \\ 1 & 1 & 0 \\ 1 & 1 & 1 \end{pmatrix}$ . Calculate  $A^{-1}$  using Gaussian elimination.

- (b) (1 point) Let  $\vec{y} = \begin{pmatrix} y_1(t) \\ y_2(t) \end{pmatrix}$ . Find the matrix  $B$  that such that  $\vec{y}' = B\vec{y}$  given

$$\begin{cases} y_1'(t) = y_1(t) + 2y_2(t) \\ y_2'(t) = y_1(t) \end{cases}$$

- (c) (3 points) Find the eigenvalues and eigenvectors of the matrix  $B$  found above.